

MATH PROBLEM OF THE WEEK

Fall 2021

Problem 8

Let a_1, a_2, a_3, \cdots be a sequence on nonnegative real numbers such that for every $n \ge 1$ we have

$$a_{n+2} \leqslant \frac{a_{n+1} + a_n}{n+2}.$$

Show that the series $\sum_{n=1}^{\infty} a_n$ converges.

We welcome solutions from everyone. The undergraduate participant from the NMSU main campus with the most correct solutions at the end of the semester will receive an award of \$500.

Solutions must be mathematically rigorous and originally obtained by the participants.

Deadline: Monday, November 15, 10 am