The Life of Jorge Martínez

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BLAST 2021

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While over his career he wrote over 110 published papers and supervised 7 Ph.D. students. His area of expertise is classified as Ordered Algebraic Structures.

Here is the list of his former PhD students.

David Kenoyer (1982) Robert T. Finn (1997) Chawne M. Kimber (1999) Erik R. Zenk (2004) Scott D. Woodward (1992) Warren Wm. McGovern (1998) Ricardo E. Carrera (2004)

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Mathematical Lineage. Paul F. Conrad (1951), Reinhold Baer (1927), Hellmuth Kneser (1921), David Hilbert (1885)

Mathematical siblings:

W. C. Holland, Michael Darnel, John Harvey III, Marlow Anderson, David Nelson, Bixler, Bleir, Byrd, Chambless, Chen, Ellis, Kenny, Lin, Lloyd, Teller.

Here is a list of journals where his work appeared.

Trans AMS Acta Mathematica Hungarica Proc. A.M.S. Archiv der Mathematik Journal of Algebra Applied Categorical Structures Topology and its Applications Order Pacific Journal of Mathematics Advances in Mathematics Mathematica Slovaca Indagationes Mathematicae Forum Mathematicum Algebra Universalis* Canadian Journal of Mathematics Journal of Pure and Applied Algebra Czechoslovak Mathematical Journal Acta Applicandae Mathematicae Rendiconti del Seminario Matematico della Universit di Padova Commentationes Mathematicae Universitatis Carolinae Tatra Mountains Mathematical Publications

(*-served as editor)

Lattice-Ordered Groups

Jorge Martínez: the early work (1969-1982)

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Jorge Martínez: the early work (1969-1982)

A lattice-ordered group is a group (G, +, 0) equipped with a lattice structure (G, \lor, \land) such that for all $a, b, c \in G$ with $a \leq b$

$$c + a \leq c + b$$
 and $a + c \leq b + c$.

We use + even though groups are not assumed to be abelian. Jorge used to classify this as an example of a *style of Conrad*.

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The most well-known examples of lattice-ordered groups: \mathbb{R} , Aut(Ω), \mathbb{Q} , \mathbb{Z} , C(X), $C(X, \mathbb{Z})$, $\mathbb{R} \times \mathbb{R}$, $\overrightarrow{\mathbb{R} \times \mathbb{R}}$, the group of divisibility of a (commutative) Bézout domain.

Lattice-Ordered Groups

One of the most important objects in ℓ -groups is the collection of its convex ℓ -subgroups: a non-empty subset $H \subseteq G$ which is a sublattice, subgroup and has the property that if $h_1 \leq g \leq h_2$ and $h_1, h_2 \in H$, then so is g.

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The collection of convex ℓ -subgroups is denoted by $\mathcal{C}(G)$. Early on, this collection was known to be a complete Brouwerian lattice. Nowadays, it is known as an example of an algebraic frame.

Lattice-Ordered Groups

A frame is a complete lattice L in which the following distributive law holds:

 $a \land \bigvee S = \bigvee \{ a \land s : s \in S \},\$

for each $a \in L$ and $S \subseteq L$.

Lattice-Ordered Groups

Topics

Variety of *l*-groups

Radicals on ℓ -groups

Torsion and quasi-torsion theories and classes of $\ell\text{-groups}$

Torsion products of ℓ -groups

Free products of ℓ -groups

Archimedean lattices

Caribbean Mathematics Foundation

Jorge Martínez: the middle stage (1985-2002)

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It was at this point in his career that Jorge took on the arduous role of Conference Organizer. This was a natural move. Others had been doing this as well.

He was instrumental in setting up the Caribbean Mathematics Foundation. Conferences were held in Curaçao; the first in 1988. Working with Charles Holland and Kluwer Academic Publishers they produced several proceedings of these conferences on ℓ -groups as well as other areas of mathematics.

Charles also was part of many other proceedings.

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In the mid 1990s, Jorge teamed up with Constantine Tsinakis to start the Consortium for Order in Algebra and Logic, a joint venture between Vanderbilt University and the University of Florida.

Caribbean Mathematics Foundation

Now is a good time to mention that Jorge also wrote a novel by the title of *For the Fragments of Justice* (1989).



Caribbean Mathematics Foundation

In this middle stage, Jorge's work started to turn from ℓ -groups to topics in ring theory with a focus on f-rings. He got into the "Dutch School" of

mathematics. He met Tony Hager.

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Topics

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Rings of continuous functions: C(X) and C(X,\mathbb{Z})
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Semiprime *f*-rings with bounded inversion

Categorical questions on *f*-rings (e.g. pushouts, monoreflections)

Bézout and Prüfer f-rings

Ring of quotients and essential extensions

Gabriel filters of ideals

Tychonoff spaces

Absolutes and Quasi F-covers of compact Hausdorff spaces

Jorge Martínez: the third stage (2002-2020)

Over the last two decades Jorge returned to working on one of his original interests: studying complete Brouwerian lattices....

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It was at this point in his career that Jorge had a command of several disparate areas of mathematics: ℓ -groups, semiprime f-rings, rings of quotients of semiprime commutative rings, Tychonoff spaces and category theory. Specifically, his understanding of these areas was focused through objects like C(G), Rad(R), dL, and zL.

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Jorge talked about this project whenever we would get together. He wrote 5 papers on the subject; the last of which left him, finally, a little bit settled.

In this third stage, Jorge's work started focused heavily on the theory of M-frames: algebraic frames with the FIP.

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Topics

Archimedean frames

Yosida frames and finitely subfit frames

Dimension theory in frames

Conrad frames

Epicompleteness in (certain) categories of frames

Nuclei on frames, and the assembly of a frame

Top 7 Articles 17

Pictures

Stories

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Hager, Anthony W.; Martinez, Jorge Fraction-dense algebras and spaces. Canad, J. Math. <u>45 (1993), no. 5</u>, 977–996.

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EXTENSIONS OF PARTIAL ORDERS ON GROUPS

A dissertation

Submitted on the eleventh day of July, 1969 to the Department of Mathematics of the Graduate School of Tulane University in partial fulfillment of the requirements for the degree of Doctor of Philosophy

by

orge Martine

Approved:

Consad

Paul F. Conrad, Chairman

Mathematics and its Applications

Jorge Martinez (Ed.)

Ordered Algebraic Structures



Ordered Algebraic Structures

Proceedings of the Caribbean Mathematics Foundation Conference on Ordered Algebraic Structures, Curaçao, August 1988

edited by

Jorge Martinez

Department of Mathematics, University of Florida, Gainesville, U.S.A.

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Ordered Algebraic Structures

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